

1. (a) What is a sequence?
 (b) What does it mean to say that $\lim_{n \rightarrow \infty} a_n = 8$?
 (c) What does it mean to say that $\lim_{n \rightarrow \infty} a_n = \infty$?

1a. sequence - ordered list of numbers

b. As n becomes large, the terms a_n approach 8

c. As n becomes large, the terms a_n become large w/o bound

2. (a) What is a convergent sequence? Give two examples.
 (b) What is a divergent sequence? Give two examples.

2a. convergent sequence ... $\lim_{n \rightarrow \infty} a_n$ exists
 examples: $a_n = \frac{1}{n}$ and $a_n = \frac{1}{2^n}$

3-12 List the first five terms of the sequence.

3. $a_n = \frac{2n}{n^2 + 1}$

4. $a_n = \frac{3^n}{1 + 2^n}$

5. $a_n = \frac{(-1)^{n-1}}{5^n}$

6. $a_n = \cos \frac{n\pi}{2}$

b. divergent sequence ... $\lim_{n \rightarrow \infty} a_n = \infty / DNE$
 examples: $a_n = n$ and $a_n = \sin(n)$

3 $\left\{ 1, \frac{4}{5}, \frac{3}{5}, \frac{8}{17}, \frac{5}{13}, \dots \right\}$

4 $\left\{ 1, \frac{9}{5}, 3, \frac{81}{17}, \frac{81}{11}, \dots \right\}$

5 $= \left\{ \frac{1}{5}, -\frac{1}{25}, \frac{1}{125}, -\frac{1}{625}, \frac{1}{3125}, \dots \right\}$

6 $= \left\{ 0, -1, 0, 1, 0, \dots \right\}$

13-18 Find a formula for the general term a_n of the sequence, assuming that the pattern of the first few terms continues.

13. $\left\{ 1, \frac{1}{3}, \frac{1}{5}, \frac{1}{7}, \frac{1}{9}, \dots \right\}$

14. $\left\{ 1, -\frac{1}{3}, \frac{1}{9}, -\frac{1}{27}, \frac{1}{81}, \dots \right\}$

15. $\left\{ -3, 2, -\frac{4}{3}, \frac{8}{9}, -\frac{16}{27}, \dots \right\}$

13 $a_n = \frac{1}{2n-1}$

14 $a_n = \left(-\frac{1}{3}\right)^{n-1}$

15 $a_n = -3 \left(-\frac{2}{3}\right)^{n-1}$