

$$A. y = \sin x + \cos(2x)$$

$$E. y = e^{x^2} + 4x - \frac{1}{\sqrt[3]{x}}$$

$$B. y = \frac{4^x}{4x-1}$$

$$F. g(x) = \frac{3}{\sec(2x)}$$

$$C. x - y^2 = 4x^3 - 1$$

$$G. h(x) = x^2 \sec(x)$$

$$D. f(x) = 3 \ln(x^2 + 2)$$

$$H. y = 4 \sqrt{\cot(\sin 3x)}$$

1. Find the slope of H in terms of x

Rewrite:  $y = 4(\cot(\sin 3x))^{1/2}$

$$H'(x) = y' = 4 \cdot \frac{1}{2} (\cot(\sin 3x))^{-1/2} \cdot -\csc^2(\sin 3x) \cdot \cos 3x \cdot 3$$

2. Find the instantaneous slope of B at  $x=0$

$$y' = \frac{(4x-1)(4^x \ln 4) - 4^x(4)}{(4x-1)^2}$$

$$y'(0) = \frac{(-1)(\ln 4) - (4)}{(-1)^2} = \boxed{-\ln 4 - 4}$$

3. Find  $\frac{d^2x}{dy^2}$  of A

$$\frac{dy}{dx} = y' = \cos x - \sin 2x \cdot 2 = \cos x - 2 \sin 2x$$

$$\frac{d^2y}{dx^2} = y'' = -\sin x - 2 \cos 2x \cdot 2 = -\sin x - 4 \cos 2x$$

4. Find the equation of the tangent line of D at  $x=1$

point:  $\boxed{(1, \ln 27)}$

slope:  $y' = 3 \cdot \frac{1}{x^2+2} \cdot 2x$

$$y'(1) = 3 \cdot \frac{1}{1+2} \cdot 2(1) = \boxed{2}$$

$$y - \ln 27 = 2(x-1)$$

5. Find the equation of the normal line of D at  $x=1$

point:  $\boxed{(1, \ln 27)}$

slope:  $\boxed{-\frac{1}{2}}$

$$y - \ln 27 = -\frac{1}{2}(x-1)$$

6. Find  $\left. \frac{dy}{dx} \right|_{(0,1)}$  for C.

$$1 - 2y \frac{dy}{dx} = 12x^2$$

$$-2y \frac{dy}{dx} = 12x^2 - 1$$

$$\frac{dy}{dx} = \frac{12x^2 - 1}{-2y}$$

$$\left. \frac{dy}{dx} \right|_{(0,1)} = \frac{12(0)^2 - 1}{-2(1)} = \frac{-1}{-2} = \frac{1}{2}$$

7. Find equation of the normal line for C at (0,1)

point:  $(0,1)$

slope:  $-2$

$$y - 1 = -2(x - 0)$$

8. Find  $F'(x)$

$$F'(x) = y' = \frac{(\sec 2x)(0) - (3)(\sec 2x \tan 2x \cdot 2)}{(\sec 2x)^2}$$

$$y' = \frac{0 \sec 2x \tan 2x}{\sec^2(2x)}$$

9. Find equation of normal line for G at  $(\pi, \pi^2)$

point:  $(\pi, \pi^2)$

$$\text{slope: } y' = (\sec x)(2x) + (x^2)(\sec x \tan x)$$

$$y'(\pi) = (\sec \pi)(2\pi) + (\pi^2)(\sec \pi \tan \pi)$$

$$= (-1)(2\pi) + (\pi^2)(-1 \cdot 0)$$

$$= -2\pi \leftarrow \text{tangent} \quad \left. \right\} = \frac{1}{2\pi} \leftarrow \text{normal}$$

$$y - \pi^2 = \frac{1}{2\pi}(x - \pi)$$

10. Find equation of tangent line for E at  $x=1$

point:  $(1, e+3)$

$$\text{slope: } y' = e^{x^2} \cdot 2x + 4 + \frac{1}{3}x^{-2/3}$$

$$y'(1) = e \cdot 2 + 4 + \frac{1}{3}$$

$$= 2e + \frac{13}{3}$$

$$y - (e+3) = \left(2e + \frac{13}{3}\right)(x - 1)$$