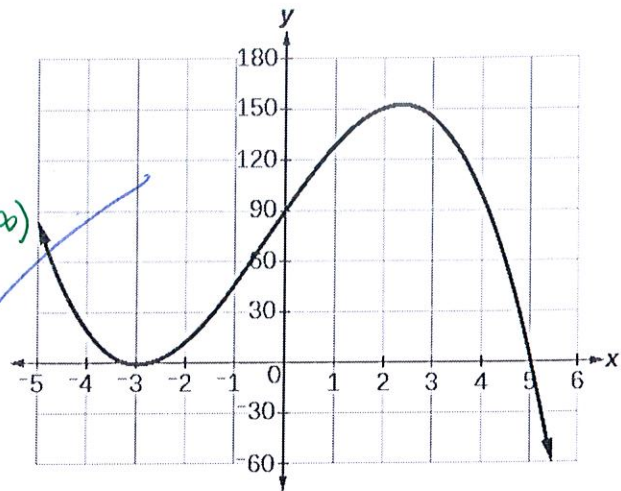


A. Consider the graph of f . Where does f have:

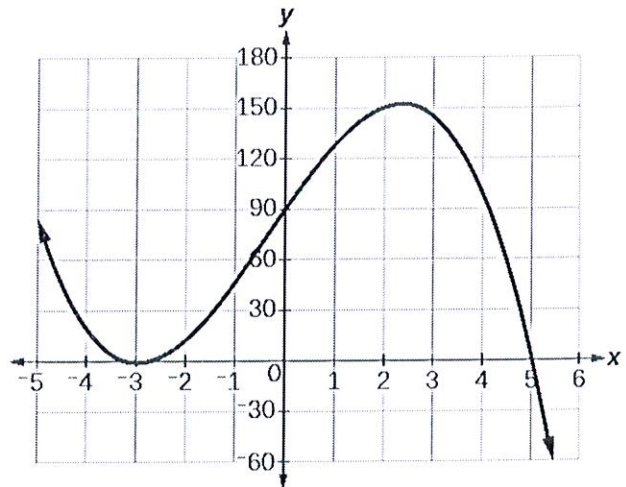
1. critical points: $x = -3, 2.5$
2. interval of increase: $(-3, 2.5)$
3. interval of decrease: $(-\infty, -3) \cup (2.5, \infty)$
4. extrema: $x = -3$ rel min
 $x = 2.5$ rel max
5. inflection point:
 $x \approx 0$
6. interval of concave up: $(-\infty, 0)$
7. interval of concave down: $(0, \infty)$



B. Consider the graph of f' , the derivative of f .

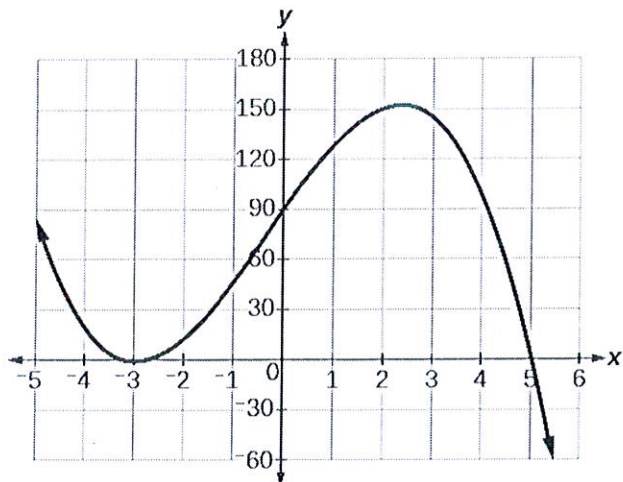
Where does f have:

1. critical points: $x = -3, 5$
2. interval of increase: $(-\infty, 5)$
3. interval of decrease: $(5, \infty)$
4. extrema: $x = 5$ rel max
5. inflection points: $x = -3, 2.5$
6. interval of concave up: $(-3, 2.5)$
7. interval of concave down: $(-\infty, -3) \cup (2.5, \infty)$



C. Consider the graph of f'' , the derivative of f' and the second derivative of f . Where does f have:

1. inflection points: $x = 5$
2. interval of concave up: $(-\infty, 5)$
3. interval of concave down: $(5, \infty)$



Function Analysis Using Derivatives and Curve Sketching

Part A: If possible, list all points on the function below which appear to meet the stated conditions. Note: There is a vertical tangent at k.

Part 2: Given the sketch of a function below, sketch the first and second derivatives on the axes provided.

- 1) $f'(x) > 0$ but finite **D, J, L, M**
- 2) $f'(x) > 0$ and $f''(x) > 0$ **J, M**
- 3) $f'(x) = 0$ and $f''(x) > 0$ **I, C**
- 4) $f'(x) = 0$ and $f''(x) < 0$ **A, E**
- 5) $f''(x) = 0$ **B, D, G, K, L**
- 6) $f(x) = 0$ and $f'(x) > 0$ **D, K**
- 7) $f'(x) = 0$ and $f''(x) = 0$ **none**
- 8) $f(x) = 0$ and $f'(x) > 0$ and $f''(x) > 0$ **none**
- 9) $f'(x) < 0$ and $f''(x) < 0$ **F**

