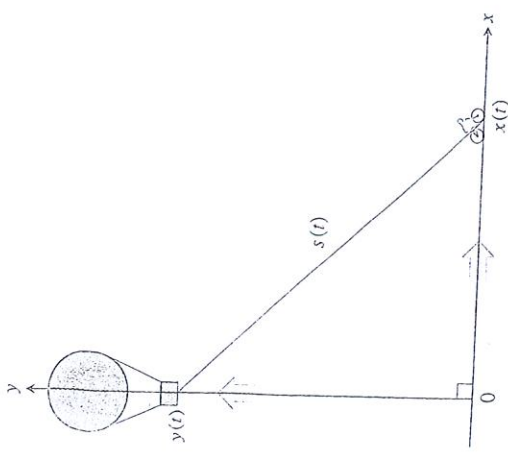
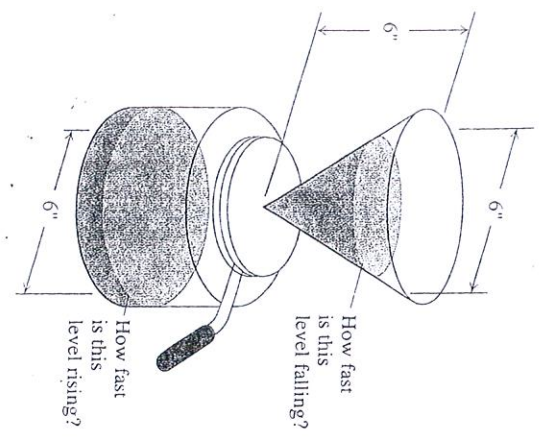


• **Rising Balloon** A balloon is rising vertically above a level, straight road at a constant rate of 1 ft/sec. Just when the balloon is 65 ft above the ground, a bicycle moving at a constant rate of 17 ft/sec passes under it. How fast is the distance between the bicycle and balloon increasing 3 sec later (see figure)?

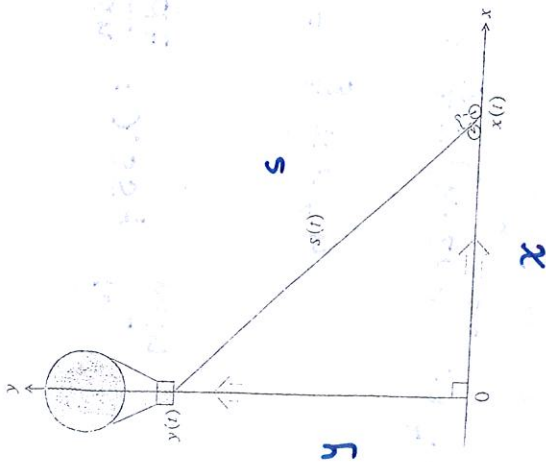


Making Coffee Coffee is draining from a conical filter into a cylindrical coffee pot at the rate of $10 \text{ in}^3/\text{min}$.

- (a) How fast is the level in the pot rising when the coffee in the cone is 5 in. deep?
- (b) How fast is the level in the cone falling at that moment?



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Equation: $x^2 + y^2 = s^2$

Derivative: $2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 2s \frac{ds}{dt}$

\uparrow 51 \uparrow 17 \uparrow 65 \uparrow 1 \uparrow Find

Substitute:

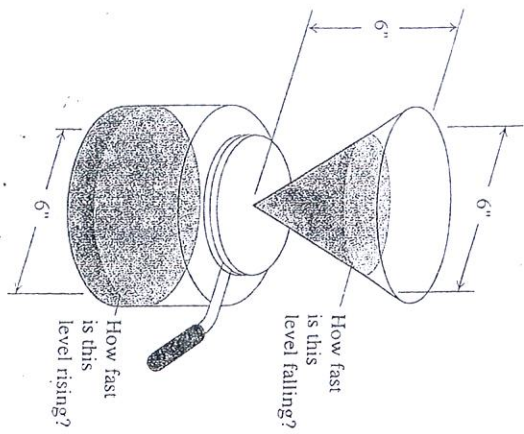
Solve:

$\frac{ds}{dt} = 11 \frac{ft}{sec}$

Making Coffee Coffee is draining from a conical filter into a cylindrical coffeepot at the rate of $10 \text{ in}^3/\text{min}$.

(a) How fast is the level in the pot rising when the coffee in the cone is 5 in. deep?

(b) How fast is the level in the cone falling at that moment?



Equation: a. $V = \pi r^2 h$

Derivative: $\frac{dV}{dt} = \pi (h \cdot 2r \frac{dr}{dt} + r^2 \frac{dh}{dt})$

Substitute: $10 \rightarrow 5 \rightarrow 3 \rightarrow 0 \rightarrow 3 \rightarrow \text{Find}$

solve:

$\frac{dh}{dt} = 0.354 \frac{\text{in}}{\text{min}}$

Equation: b. $V = \frac{1}{3} \pi r^2 h$

realized missing $\frac{dr}{dt}$
 ~~$\frac{dV}{dt} = \frac{1}{3} \pi (h \cdot 2r \frac{dr}{dt} + r^2 \frac{dh}{dt})$~~

~~$-10 \rightarrow 5 \rightarrow 3 \rightarrow ? \rightarrow 3 \rightarrow \text{Find}$~~

Equation (simplified): $V = \frac{1}{3} \pi (\frac{1}{2}h)^2 h$

$V = \frac{\pi}{12} h^3$

Derivative: $\frac{dV}{dt} = \pi h^2 \frac{dh}{dt}$

Substitute: $-10 \rightarrow 4 \rightarrow 5 \rightarrow \text{Find}$

solve:

$dh = -0.25 \frac{\text{in}}{\text{min}}$