

Algebra 1
Interpreting Structure in Expressions

Name: _____

Definitions:

_____ : a letter that stands for a particular numerical value.

_____ : is a mathematical expression that consists of variables, numbers and operations.

_____ : a product of numbers and variables in an algebraic expression.

_____ : numbers or quantities you can multiply together to get another number/quantity.

_____ : A number used to multiply a variable.

_____ : A fixed value.

Caroline signs up for an online service to watch her favorite movies. The service costs \$12.00 to begin and then Caroline must pay \$3.50 per movie she watches. The **algebraic expression** below models her total cost.

$$\underbrace{12.00} + \underbrace{3.50x}$$

"x" represents the _____

Factors: _____ Coefficient: _____ Constant: _____

Example 1

Tara and two friends had dinner at a Spanish tapas restaurant that charged \$6 per tapa, or appetizer. The three of them shared several tapas. The total bill included taxes of \$4.32. What are the terms, factors, and coefficients of the algebraic expression that represents the number of tapas ordered?

Algebraic Expression: _____ Terms: _____

Factors: _____ Coefficient: _____ Constant: _____

Example 2

The difference of seven and five times a number.

Algebraic Expression: _____ Terms: _____

Factors: _____ Coefficient: _____ Constant: _____

Example 3

Stephanie wants to buy 4 purses that are on sale for 30% off the original price. Write an expression that represents the total cost of the purses. Let x represent the cost of one purse.

DISCOUNT PROBLEM: _____

Algebraic Expression: _____ Terms: _____

Factors: _____ Coefficient: _____ Constant: _____

You try these! ☺

Name the terms, factors, coefficients, and constants in the following algebraic expressions:

1. $3x + 5$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

2. $-6x + 4$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

3. $2j + 3k + 6m$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

4. $12x - 0.25$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

5. $100 - 3x + 12y$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

6. $4x^3 + x^2 - 15$

Terms: _____

Factors: _____

Coefficients: _____

Constants: _____

Translate each algebraic expression into a verbal expression.

6. $8 + 3x$ _____
7. $5m - 7$ _____
8. $x^2 + 100$ _____

Translate each verbal expression into an algebraic expression.

9. The sum of a number and 10. 10. The product of 9 and x squared.
11. Nine less than g to the fourth power. 12. Eight more than 3 times a number
13. Three-fourths the square of a number 14. Two times the quotient of 12 and a number
15. 15 less than twice a number
16. The product of 5 and the cube of a number increased by the difference of 6 and x
17. Half the sum of x and y decreased by one-third y

Write an algebraic expression to describe each situation. Identify the terms, factors, coefficients, and constants.

1. Sarah is opening a new taxi service in Atlanta. It costs \$4.50 to ride in her taxi plus \$0.75 per mile driven.

Algebraic Expression: _____ Terms: _____
Factors: _____ Coefficients: _____
Constants: _____

2. Shane agrees to buy a package deal of monthly gym passes, and in turn receives a 15% discount. Write an algebraic expression to represent the total cost of the package with the discount, if x represents the cost of the package. ** Please simplify first!

DISCOUNT PROBLEMS: _____
Algebraic Expression: _____ Terms: _____
Factors: _____, Coefficients: _____
Constants: _____

Name _____ Date _____ Period _____

Why Did the Cow Keep Jumping Over the Barrel?

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	

Translate each phrase below into an algebraic expression and find your answer in the corresponding answer column. Write the letter of that exercise in the box that contains the number of the answer.

E	3 times a number	18	$x + 3$	S	5 times a number, increased by 8	22	$8(x + 5)$
O	3 more than a number	15	$3x - 8$	A	5 times the sum of a number and 8	4	$8(2x + 5)$
S	3 decreased by a number	19	$x - 3$	H	5 more than 8 times a number	2	$8x + 5$
R	3 less than a number	12	$3x + 8$	O	8 times the sum of a number and 5	13	$2(5x + 8)$
A	one third of a number	3	$3x$	C	Twice the sum of 5 times a number and 8	6	$5x + 8$
I	8 more than 3 times a number	25	$3 - x$	T	2 more than five eighths of a number	20	$5(x + 8)$
N	8 less than 3 times a number	5	$x/3$	W	8 times the sum of twice a number and 5	11	$5/8x + 2$
A	7 less than 4 times a number	1	$7 - 4x$	T	9 meters higher than altitude x	7	$x + 15$
S	7 decreased by 4 times a number	16	$2x - 9$	F	15 meters per second slower than speed x	28	$x + 9$
G	9 less than twice a number	14	$7x + 4$	P	15 degrees hotter than temperature x	26	$4x - 9$
N	9 decreased by twice a number	9	$4x - 7$	O	9 meters shorter than twice length x	23	$2x - 9$
O	9 less than half a number	8	$7x + 4x$	C	9 years older than twice age x	10	$2x + 9$
I	7 times a number, increased by 4	24	$9 - 2x$	H	\$9 cheaper than 4 times price x	17	$x - 15$
R	7 times a number, increased by 4 times the number	27	$x/2 - 9$	M	9 centimeters less than three fourths of length x	21	$3/4x - 9$

Adding and Subtracting Polynomials

Simplify each expression.

1) $(5p^2 - 3) + (2p^2 - 3p^3)$

2) $(a^3 - 2a^2) - (3a^2 - 4a^3)$

3) $(4 + 2n^3) + (5n^3 + 2)$

4) $(4n - 3n^3) - (3n^3 + 4n)$

5) $(3a^2 + 1) - (4 + 2a^2)$

6) $(4r^3 + 3r^4) - (r^4 - 5r^3)$

7) $(5a + 4) - (5a + 3)$

8) $(3x^4 - 3x) - (3x - 3x^4)$

9) $(-4k^4 + 14 + 3k^2) + (-3k^4 - 14k^2 - 8)$

10) $(3 - 6n^5 - 8n^4) - (-6n^4 - 3n - 8n^5)$

11) $(12a^5 - 6a - 10a^3) - (10a - 2a^5 - 14a^4)$

12) $(8n - 3n^4 + 10n^2) - (3n^2 + 11n^4 - 7)$

13) $(-x^4 + 13x^5 + 6x^3) + (6x^3 + 5x^5 + 7x^4)$

14) $(9r^3 + 5r^2 + 11r) + (-2r^3 + 9r - 8r^2)$

15) $(13n^2 + 11n - 2n^4) + (-13n^2 - 3n - 6n^4)$

16) $(-7x^5 + 14 - 2x) + (10x^4 + 7x + 5x^5)$

When multiplying TWO polynomials together you are _____ all the terms in the first polynomial to all the terms in the second polynomial.

1. $(2x - 3)(4x + 5)$

2. $(3x + 7)(x^2 - 2x + 5)$

Binomial x Binomial

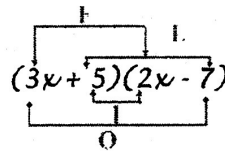
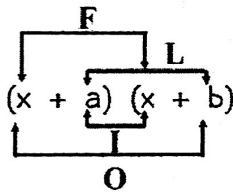
1. Multiply: $(3x + 5)(2x - 7)$

F- _____

O- _____

I- _____

L- _____



Now you try!

2. Multiply: $(2x + 4)(x + 6)$

3. Multiply: $(3x - 5)(5x^2 - x + 2)$

4. Multiply: $(4x - 3)(3x^3 - 2x^2 + 5)$

5. $(x+2)^2$

Multiplying Polynomials

Find each product.

1) $6v(2v + 3)$

2) $7(-5v - 8)$

3) $2x(-2x - 3)$

4) $-4(v + 1)$

5) $(2n + 2)(6n + 1)$

6) $(4n + 1)(2n + 6)$

7) $(x - 3)(6x - 2)$

8) $(8p - 2)(6p + 2)$

9) $(6p + 8)(5p - 8)$

10) $(3m - 1)(8m + 7)$

11) $(2a - 1)(8a - 5)$

12) $(5n + 6)(5n - 5)$

Multiplying Special Case Polynomials

Find each product.

1) $(x + 5)(x - 5)$

2) $(n - 1)(n + 1)$

3) $(p - 1)^2$

4) $(x - 3)(x + 3)$

5) $(x - 4)^2$

6) $(n + 3)^2$

7) $(x - 5)(x + 5)$

8) $(n - 5)^2$

9) $(2k^2 + 1)^2$

10) $(8a^2 + 4)(8a^2 - 4)$

11) $(2 + 5n^2)^2$

12) $(3x - 7)(3x + 7)$

Simplify the following polynomials.

1. $(3x + 5) + (4 - x)$

2. $(2x^2 - 6x + 3) - (5x^2 - 6)$

3. $25(2y^3 + 3y^2 + 4)$

4. $6x^2(3x^2 + 5x)$

5. $(a + 2)(5a - 4)$

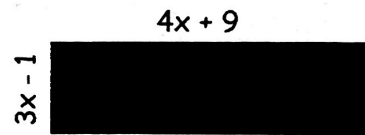
6. $(x - 3)^2$

Applications with Polynomials

Perimeter - _____

Area - _____

Volume - _____



7. Find the perimeter of the rectangle above. (**Perimeter** = _____)

8. Find the area of the rectangle above. (**Area of a rectangle is A** = _____)

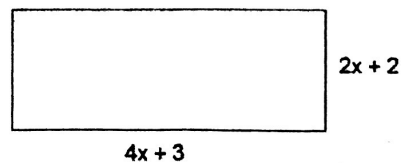
9. Find the volume of a cube whose side length is $x + 1$.

(**Volume of a cube is V** = _____)

10. Find the perimeter and area of the rectangle to the right.

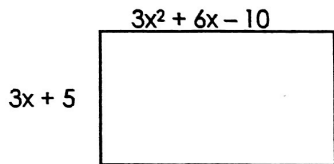
P = _____

A = _____

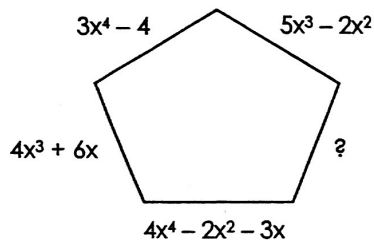


Finding Perimeter and Area Using Polynomials

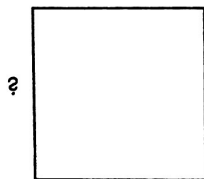
1. What is the distance around the rectangle if the length is $3x^2 + 6x - 10$ and the width is $3x + 5$?



2. If the perimeter of the pentagon below is $7x^4 + 9x^3 - 6x^2 + 10$, what is the length of the missing side?



3. If the perimeter of the **square** below is $12x^5 - 8x^2 + 20x - 4$, what is the length of one side?



4. Ana knows that the perimeter of her backyard is $(6x^2 + 14x)$ feet. If the length of her backyard is $(2x^2 + 3x - 7)$ feet, what is the width of her backyard?